## Mathematics Department

## Grade 5

Developed by: Leann Martin \& Grade 5 Teachers
Supported by: Dana Neri
Effective Date: September 2023

## Scope and Sequence

| Month | Grade 5 |  |
| :--- | :--- | :--- |
| September | Grade 5 Math Baseline Assessment <br> Chapter 1: Whole Numbers and the Four Operations <br> October <br> November <br> Chapter 2: Fractions and Mixed Numbers <br> Chapter 3: Multiplying and Dividing Fractions and Mixed <br> Numbers | Strategies Interventions: <br> Bridges Volume 5 <br> (Multiplication Facts), <br> Volumes 6 and 7 (Word <br> Problems) |
| December | Finish Chapter 3 <br> Grade 5 Benchmark Assessment 1 (by November 30) <br> (Chapters 1 through 3) <br> Chapter 4: Decimals | Strategies Interventions: <br> Bridges Volume 8 |
| January | Finish Chapter 4 <br> Chapter 5: Four Operations of Decimals- When estimate <br> decimal x decimal, show process for exact answer; OR- change to <br> fraction and multiply For division- encourage students to change <br> to fraction and divide (5.NBT..7) | Strategies Interventions: <br> Bridges Volume 9 |
| February | Grade 5 Benchmark Assessment 2- Fractions and Decimals <br> Book B: Chapter 6: Volume |  |


| March | Grade 5 Math Spring Summative Assessment <br> Chapter 7: Line Plots and the Coordinate Plane |  |
| :--- | :--- | :--- |
| April | Chapter 8: Polygons <br> Speak to Grade 4 - ask about completion of Chapter 8 <br> (Polygons and Symmetry) Pull from Grade 4 Chapter 8 as <br> needed. <br> Grade 5 Benchmark Assessment 3 New: Chapters 6 through 8 |  |
| May | Chapter 9: Ratio (in preparation for Grade 6) |  |
| June | Chapter 10: Percent (In preparation for grade 6) |  |


| Unit 1 |  |
| :---: | :---: |
| Whole Numbers |  |
| Summary and Rationale |  |
| In this unit, students represent six-digit and seven-digit numbers in word, standard, and expanded forms. They extend place-value to larger numbers as they compare and order. <br> Students extend what they have learned about multiplication to larger numbers. They multiply and divide using patterns within multiples of 10 and conventional algorithms. <br> Students simplify numerical expressions using order of operations, and solve real-world problems involving multiplication and division using pictorial representations and other strategies. |  |
|  | Recommended Pacing |
| Math in Focus Chapter 1: Whole Numbers and the Four Operations |  |
|  | Standards |
| Numbers \& Operations in Base Ten |  |
| 5.NBT. 1 | Recognize that in a multi-digit number, a digit in one place represents 10 times as much as it represents in the place to its right and $1 / 10$ of what it represents in the place to its left. |
| 5.NBT. 2 | Explain patterns in the number of zeros of the product when multiplying a number by powers of 10 , and explain patterns in the placement of the decimal point when a decimal is multiplied or divided by a power of 10 . Use whole-number exponents to denote powers of 10 . |
| 5.NBT. 5 | Fluently multiply multi-digit whole numbers using the standard algorithm. |
| 5.NBT. 6 | Find whole-number quotients of whole numbers with up to four-digit dividends and two-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models. |
| Operations \& Algebraic Thinking |  |
| 5.OA. 1 | Use parentheses, brackets, or braces in numerical expressions and evaluate expressions with these symbols. |


| 5.OA. 2 | Write simple expressions that record calculations with numbers, and interpret numerical expressions without evaluating them. For example, express the calculation "add 8 and 7 , then multiply by 2 " as 2 $\times(8+7)$. Recognize that $3 \times(18932+921)$ is three times as large as $18932+921$, without having to calculate the indicated sum or product. |
| :---: | :---: |
| Mathematical Practices |  |
| K-12.MP. 1 | Make sense of problems and persevere in solving them. |
| K-12.MP. 2 | Reason abstractly and quantitatively. |
| K-12.MP3 | Construct viable arguments and critique the reasoning of others. |
| K-12.MP. 4 | Model with mathematics. |
| K-12.MP. 5 | Use appropriate tools strategically. |
| K-12.MP. 6 | Attend to precision. |
| K-12.MP. 7 | Look for and make use of structure. |
| K-12.MP. 8 | Look for and express regularity in repeated reasoning. |
| Interdisciplinary Connections |  |
| ELA |  |
| Math journal, math vocabulary discussions, reading topic-related books, providing explanations |  |
| SL.1.1. | Participate in collaborative conversations with diverse partners about grade 1 topics and texts with peers and adults in small and larger groups. A. Follow agreed-upon norms for discussions (e.g., listening to others with care, speaking one at a time about the topics and texts under discussion). B. Build on others' talk in conversations by responding to the comments of others through multiple exchanges. C. Ask questions to clear up any confusion about the topics and texts under discussion. |
| SL.1.3. | Ask and answer questions about what a speaker says in order to gather additional information or clarify something that is not understood. |
| SL.1.6. | Produce complete sentences when appropriate to task and situation. |
| Integration of Technology |  |
| Use of SmartBoard, playing online games |  |
| 8.1.2.A. 4 | Demonstrate developmentally appropriate navigation skills in virtual environments (i.e. games, museums). |


| Career Readiness, Life Literacies and Key Skills |  |  |
| :---: | :---: | :---: |
| 9.1.5.CR.1 | Compare various ways to give back and relate them to your strengths, interests, and other personal factors. |  |
| 9.2.5.CAP. 1 | Evaluate personal likes and dislikes and identify careers that might be suited to personal likes. |  |
| 9.2.5.CAP. 2 | Identify how you might like to earn an income. |  |
| 9.2.5.CAP. 3 | Identify qualifications needed to pursue traditional and non-traditional careers and occupations. |  |
| 9.2.5.CAP. 4 | Explain the reasons why some jobs and careers require specific training, skills, and certification (e.g., life guards, child care, medicine, education) and examples of these requirements. |  |
| 9.2.5.CI. 3 | Participate in a brainstorming session with individuals with diverse perspectives to expand one's thinking about a topic of curiosity. |  |
| 9.2.5.CT. 1 | Identify and gather relevant data that will aid in the problem-solving process. |  |
| 9.2.5.CT. 2 | Identify a problem and list the types of individuals and resources (e.g., school, community agencies, governmental, online) that can aid in solving the problem. |  |
| 9.2.5.CT. 3 | Describe how digital tools and technology may be used to solve problems. |  |
| 9.2.5.CT. 4 | Apply critical thinking and problem-solving strategies to different types of problems such as personal, academic, community and global. |  |
| 9.4.5.TL. 1 | Compare the common uses of at least two different digital tools and identify the advantages and disadvantages of using each. |  |
| Instructional Focus |  |  |
| Enduring Un | erstandings: | Essential Questions: |
| Whole numb <br> Numbers according to <br> Patterns can divide numb <br> Numerical exp order of ope | s can be written in different ways. <br> be compared and rounded, eir place value. <br> used to help you multiply and ressions can be simplified using the ions. | Where do we use large numbers in real-world situations? <br> Why are the four operations of whole numbers important in everyday life? <br> What is the order of operations and why is it necessary? <br> What kind of number patterns can help when multiplying and dividing by multiples of 10 ? |

Multiplication and division can be used to solve
real-world problems.
Evidence of Learning (Assessments)
Math in Focus Assessment Guide Chapter 1: Whole Numbers and the Four Operations
Math in Focus Cumulative Review 1 (Chapters 1 through 3)
Benchmark Assessments

## Objectives (SLO)

Students will know:

- Hundred, thousand
- Million
- Place-value
- Greater than (>), less than (<)
- Product, factor
- Quotient, dividend, divisor, remainder
- Numerical expression
- Order of operations

Students will be able to:

- Count by ten thousands and hundred thousands to 10,000,000.
- Read and write numbers to $10,000,000$ in standard form, in word form, and in expanded form.
- Identify the place value of any digit in numbers to $10,000,000$.
- Multiply and divide numbers by 10,100 , or 1,000 using patterns.
- Multiply and divide numbers up to 4 digits by multiples of 10,100 , or 1,000 .
- Multiply whole numbers by 10 squared or 10 cubed.
- Multiply and divide a 2,3 , or 4 -digit number by a 2 digit number.
- Multiply by a 2-digit fluently
- Divide by a 2-digit fluently.
- Use order of operations to simplify a numerical expression.
- Evaluate numerical expressions with parentheses, brackets, and braces.
- Use efficient strategies to solve multi-step problems involving multiplications and division.
- Express and interpret the product or quotient appropriately.


## Suggested Resources/Technology Tools

Math in Focus Resources Chapter 1: Whole Numbers and the Four Operations
Resources and Manipulatives
Place-value chips
Place-value charts
Number lines
Calculators
Multiplication tables
Division tables
Number cards

Symbol cards
Numerical expressions table

## Online Resources

HMH Ed: Your Friend in Learning
www.funbrain.com/tens/index.html (Place value)
www.gamequarium.com/estimation.html (Estimation)
www.mathplayground.com/division02.html (Division with remainders)
www.kidsnumbers.com/long-division.php (Division practice games)
www.mathplayground.com/WordProblemsWithKatie2.html (Multiplication and division number stories)
www.math-play.com/Order-of-Operations-Millionaire/order-of-operations-millionaire.html (Order of operations)

Literacy Connections
Counting on Frank by Rod Clement
How Much is a Million? by David M. Schwartz
Math Talk by Theoni Pappas
Speed Mathematics by Bill Handley
A Remainder of One by Elinor J. Pinczes
One Hundred Hungry Ants by Elinor J. Pinczes

## Tier 1 Modifications and Accommodations

Including special education students, Multilingual Language Learners (MLLs), students at risk of school failure, gifted and talented students, and students with 504 plans;

## General Modifications for students struggling to learn:

Small group instruction within the classroom
Differentiation through content, process, product, and environment
Individual feedback and praise towards what is done correctly based upon effort, attitude and strategy.
Help students manage individual stressors for the student and plan alternate pathways for completion of assignments
Special Education - Reteach/Extra practice workbook pages, anchor charts, scaffolded explanations of topics, manipulatives, additional time for work, group work, visual aids, modeling, hands-on learning activities, small group work for more individualized attention
*These are only suggested ideas to modify instruction, modifications and accommodations should be tailored to each student's IEP and needs. Also, see textbook for Differentiated Instruction ideas in each chapter.

504 - Reteach/Extra practice pages, anchor charts, scaffolded explanations of topics, manipulatives, extra time for work, group work, visual aids, modeling, hands-on learning activities, small group work for more individualized attention

MLL - Select activities which reinforce chapter vocabulary and connections among these words such as:
A Word Wall which includes terms, definitions, and examples
Drawings and numbers to show examples of terms
Gifted and Talented - Enrichment workbook, Put on Your Thinking Cap pages and resources, higher-level questions, challenge packets, KenKen and other puzzles, leading group work

## Career Readiness, Life Literacies, and Key Skills NJSLS

Please select all standards that apply to this unit of study:
Act as a responsible and contributing community members and employee
Attend to financial well-being
Consider the environmental, social and economic impacts of decisions
Demonstrate creativity and innovation
Utilize critical thinking to make sense of problems and persevere in solving them
Model integrity, ethical leadership and effective management
Plan education and career paths aligned to personal goals
Use technology to enhance productivity increase collaboration and communicate effectively
Work productively in teams while using cultural/global competence
Suggestions on integrating these standards can be found at: https://www.nj.gov/education/standards/clicks

| Unit 2 |
| :--- |
| $\quad$ Fractions \& Mixed Numbers |
| $\quad$ Summary and Rationale | | In this unit, students learn to add and subtract unlike fractions and mixed numbers by rewriting the fractions |
| :--- |
| as like fractions using the concept of least common denominator and equivalent fractions. Fraction circles |
| and bar models are used to illustrate the concepts. Students apply their knowledge of finding common factors |
| and multiples to add and subtract unlike but related fractions. They are encouraged to recognize the |
| relationships between fractions, mixed numbers, division expressions, and decimals. Learning to represent |
| the same number in different ways is a necessary skill for the study of algebra. |
| Students learn how to multiply and divide whole numbers, proper fractions, improper fractions, and mixed |
| numbers in any combinations. Using manipulatives such as fraction bars and circles or using the pictorial |
| approach by drawing bar models are ideal ways of demonstrating the concepts. |


|  | share a 50-pound sack of rice equally by weight, how many pounds of rice should each person get? Between what two whole numbers does your answer lie? |
| :---: | :---: |
| 5.NF. 4 | Apply and extend previous understandings of multiplication to multiply a fraction or whole number by a fraction. |
| 5.NF.4a | Interpret the product $(a / b) \times q$ as a part of a partition of $q$ into $b$ equal parts; equivalently, as the result of a sequence of operations $a \times q \div b$. For example, use a visual fraction model to show ( $2 / 3$ ) $\times 4=$ $8 / 3$, and create a story context for this equation. Do the same with $(2 / 3) \times(4 / 5)=8 / 15$. (In general, $(a / b) \times(c / d)=a c / b d$. |
| 5.NF.4b | Find the area of a rectangle with fractional side lengths by tiling it with unit squares of the appropriate unit fraction side lengths, and show that the area is the same as would be found by multiplying the side lengths. Multiply fractional side lengths to find areas of rectangles, and represent fraction products as rectangular areas. |
| 5.NF. 5 | Interpret multiplication as scaling (resizing), by: |
| 5.NF.5a | Comparing the size of a product to the size of one factor on the basis of the size of the other factor, without performing the indicated multiplication. |
| 5.NF.5b | Explaining why multiplying a given number by a fraction greater than 1 results in a product greater than the given number (recognizing multiplication by whole numbers greater than 1 as a familiar case); explaining why multiplying a given number by a fraction less than 1 results in a product smaller than the given number; and relating the principle of fraction equivalence $a / b=(n \times a) /(n \times b)$ to the effect of multiplying $a / b$ by 1 . |
| 5.NF. 6 | Solve real world problems involving multiplication of fractions and mixed numbers, e.g., by using visual fraction models or equations to represent the problem. |
| 5.NF. 7 | Apply and extend previous understandings of division to divide unit fractions by whole numbers and whole numbers by unit fractions. ${ }^{1}$ |
| 5.NF.7a | Interpret division of a unit fraction by a non-zero whole number, and compute such quotients. For example, create a story context for $(1 / 3) \div 4$, and use a visual fraction model to show the quotient. Use the relationship between multiplication and division to explain that $(1 / 3) \div 4=1 / 12$ because (1/12) $\times$ $4=1 / 3$. |
| 5.NF.7b | Interpret division of a whole number by a unit fraction, and compute such quotients. For example, create a story context for $4 \div(1 / 5)$, and use a visual fraction model to show the quotient. Use the relationship between multiplication and division to explain that $4 \div(1 / 5)=20$ because $20 \times(1 / 5)=4$. |
| 5.NF.7c | Solve real world problems involving division of unit fractions by non-zero whole numbers and division of whole numbers by unit fractions, e.g., by using visual fraction models and equations to represent the problem. For example, how much chocolate will each person get if 3 people share $1 / 2 \mathrm{lb}$ of chocolate equally? How many 1/3-cup servings are in 2 cups of raisins? |
| Mathematical Practices |  |
| K-12.MP. 1 | Make sense of problems and persevere in solving them. |


| K-12.MP. 2 | Reason abstractly and quantitatively. |
| :---: | :---: |
| K-12.MP3 | Construct viable arguments and critique the reasoning of others. |
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| K-12.MP. 5 | Use appropriate tools strategically. |
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| K-12.MP. 7 | Look for and make use of structure. |
| K-12.MP. 8 | Look for and express regularity in repeated reasoning. |
| Interdisciplinary Connections |  |
| ELA |  |
| Math journal, math vocabulary discussions, reading topic-related books, providing explanations |  |
| SL.1.1. | Participate in collaborative conversations with diverse partners about grade 1 topics and texts with peers and adults in small and larger groups. A. Follow agreed-upon norms for discussions (e.g., listening to others with care, speaking one at a time about the topics and texts under discussion). B. Build on others' talk in conversations by responding to the comments of others through multiple exchanges. C. Ask questions to clear up any confusion about the topics and texts under discussion. |
| SL.1.3. | Ask and answer questions about what a speaker says in order to gather additional information or clarify something that is not understood. |
| SL.1.6. | Produce complete sentences when appropriate to task and situation. |
| Integration of Technology |  |
| Use of SmartBoard, playing online games |  |
| 8.1.2.A.4 | Demonstrate developmentally appropriate navigation skills in virtual environments (i.e. games, museums). |
| Career Readiness, Life Literacies and Key Skills |  |
| 9.1.5.CR.1 | Compare various ways to give back and relate them to your strengths, interests, and other personal factors. |
| 9.2.5.CAP. 1 | Evaluate personal likes and dislikes and identify careers that might be suited to personal likes. |


| 9.2.5.CAP. 2 | Identify how you might like to earn an income. |  |
| :---: | :---: | :---: |
| 9.2.5.CAP. 3 | Identify qualifications needed to pursue traditional and non-traditional careers and occupations. |  |
| 9.2.5.CAP. 4 | Explain the reasons why some jobs and careers require specific training, skills, and certification (e.g., life guards, child care, medicine, education) and examples of these requirements. |  |
| 9.2.5.CI. 3 | Participate in a brainstorming session with individuals with diverse perspectives to expand one's thinking about a topic of curiosity. |  |
| 9.2.5.CT. 1 | Identify and gather relevant data that will aid in the problem-solving process. |  |
| 9.2.5.CT. 2 | Identify a problem and list the types of individuals and resources (e.g., school, community agencies, governmental, online) that can aid in solving the problem. |  |
| 9.2.5.CT. 3 | Describe how digital tools and technology may be used to solve problems. |  |
| 9.2.5.CT. 4 | Apply critical thinking and problem-solving strategies to different types of problems such as personal, academic, community and global. |  |
| 9.4.5.TL. 1 | Compare the common uses of at least two different digital tools and identify the advantages and disadvantages of using each. |  |
| Instructional Focus |  |  |
| Enduring Un | erstandings: | Essential Questions: |
| To add or common mult that as the de <br> Unlike fracti and subtract same denom <br> Whole numb can be multi <br> Dividing a equivalent to the whole nu | subtract unlike fractions, find a iple of both denominators and use ominator of both fractions. <br> s and mixed numbers can be added by first rewriting them with the ators. <br> rs, fractions, and mixed numbers ied or divided in any combination. <br> fraction by a whole number is multiplying it by the reciprocal of ber. | What is the first step in adding or subtracting unlike fractions or mixed numbers? <br> How do you add or subtract unlike fractions and mixed numbers? <br> How do you multiply fractions, mixed numbers and whole numbers? <br> How do the factors affect the product if one of the factors is a fraction? <br> Does the order in which you multiply matter? <br> How do you divide fractions, mixed numbers and whole numbers? |

## Evidence of Learning (Assessments)

Math in Focus Assessment Guide Chapter 2: Fractions and Mixed Numbers
Math in Focus Assessment Guide Chapter 3: Multiplying and Dividing Fractions and Mixed Numbers
Math in Focus Cumulative Review 1 (Chapters 1 through 3)
Benchmark Assessments
Objectives (SLO)

Students will know:

- Numerator, denominator
- Equivalent fraction
- Unlike Fraction
- Multiple, least common multiple (LCM)
- Least common denominator
- Simplest form
- Benchmarks
- Fraction bar
- Division expression
- Mixed number
- Product, common factor
- Proper fraction, improper fraction
- Reciprocal

Students will be able to:

- Understand and apply the relationships among fractions, mixed numbers and division expressions
- Find equivalent fractions..
- Add and subtract two unlike fractions where one denominator is not a multiple of the other.
- Estimate sums of fractions and differences between fractions.
- Add and subtract mixed numbers with or without renaming.
- Estimate sums and differences of mixed numbers
- Express fractions, division expressions, and mixed numbers as decimals.
- Solve real-world problems involving addition and subtraction of fractions and mixed numbers..
- Multiply proper fractions by whole numbers
- Multiply improper fractions by whole numbers.
- Multiply proper fractions.
- Multiply improper fractions by proper and improper fractions.
- Multiply a mixed number by a whole number.
- Multiple a mixed number by a mixed number
- Compare the size of a product to the size of its factors.
- Divide a fraction by a whole number.
- Divide a whole number by a unit fraction.
- Solve real-world problems involving multiplication and division of whole numbers, proper fractions, improper fractions, and mixed numbers.


## Suggested Resources/Technology Tools

Math in Focus Resources Chapter 2: Fractions and Mixed Numbers
Math in Focus Resources Chapter 3: Multiplying and Dividing Fractions and Mixed Numbers
Resources and Manipulatives
Fraction circles
Fraction Tiles
Grid paper

HMH Ed: Your Friend in Learning
www.aaamath.com/fra43ax2.htm (Comparing fractions with like denominators)
www.aaamath.com/fra43bx2.htm (Comparing fractions with unlike denominators)
www.funbrain.com/fract/index.html (Equivalent fraction game)
www.math-play.com/adding-and-subtracting-fractions-game.html (Adding and subtracting fraction game)
www.everydaymathonline.com
www.aaamath.com/fra66dx2.htm (Adding mixed numbers)
www.aaamath.com/fra66ex2.htm (Subtracting mixed numbers)
www.mathplayground.com/fractions_mult.html (Multiplying fractions)

Literacy Connections
Gator Pie by Louise Matthews
Eating Fractions by Bruce McMillian
Fourscore and 7: Investigating in American History by Betsy Franco
Tiger Math by Ann Whitehead Nagda
Jim and the Beanstalk by Jean Cushman
Fraction Action by Loreen Leedy

## Tier 1 Modifications and Accommodations

Including special education students, Multilingual Language Learners (MLLs), students at risk of school failure, gifted and talented students, and students with 504 plans;

## General Modifications for students struggling to learn:

Small group instruction within the classroom
Differentiation through content, process, product, and environment
Individual feedback and praise towards what is done correctly based upon effort, attitude and strategy.
Help students manage individual stressors for the student and plan alternate pathways for completion of assignments

Special Education - Reteach/Extra practice workbook pages, anchor charts, scaffolded explanations of topics, manipulatives, additional time for work, group work, visual aids, modeling, hands-on learning activities, small group work for more individualized attention
*These are only suggested ideas to modify instruction, modifications and accommodations should be tailored to each student's IEP and needs. Also, see textbook for Differentiated Instruction ideas in each chapter.

504 - Reteach/Extra practice pages, anchor charts, scaffolded explanations of topics, manipulatives, extra time for work, group work, visual aids, modeling, hands-on learning activities, small group work for more individualized attention

MLL - Select activities which reinforce chapter vocabulary and connections among these words such as:
A Word Wall which includes terms, definitions, and examples
Drawings and numbers to show examples of terms

Gifted and Talented - Enrichment workbook, Put on Your Thinking Cap pages and resources, higher-level questions, challenge packets, KenKen and other puzzles, leading group work

## Career Readiness, Life Literacies, and Key Skills NJSLS

Please select all standards that apply to this unit of study:
Act as a responsible and contributing community members and employee
Attend to financial well-being
Consider the environmental, social and economic impacts of decisions
Demonstrate creativity and innovation
Utilize critical thinking to make sense of problems and persevere in solving them
Model integrity, ethical leadership and effective management
Plan education and career paths aligned to personal goals
Use technology to enhance productivity increase collaboration and communicate effectively
Work productively in teams while using cultural/global competence
Suggestions on integrating these standards can be found at: https://www.nj.gov/education/standards/clicks

## Unit 3

## Decimals

## Summary and Rationale

In this unit, students are introduced to the place value of decimals through thousandths. In the process, they learn how to read and write decimals through thousandths, identify the relationship between fractions and decimals, compare and order decimals, and round decimals to the nearest hundredth.

Students use patterns to help them multiply and divide decimals by one-digit whole numbers. They also learn conventional algorithms for adding, subtracting, multiplying, and dividing decimals and solve problems involving decimals, including multi-step problems..

## Recommended Pacing

Math in Focus Resources Chapter 4: Decimals
Math in Focus Resources Chapter 5: Four Operations of Decimals

## Standards

Numbers \& Operations in Base Ten

| 5.NBT.3 | Read, write, and compare decimals to thousandths. |
| :--- | :--- |
| 5.NBT.3a | Read and write decimals to thousandths using base-ten numerals, number names, and expanded form, <br> e.g., $347.392=3 \times 100+4 \times 10+7 \times 1+3 \times(1 / 10)+9 \times(1 / 100)+2 \times(1 / 1000)$. |
| 5.NBT.3b | Compare two decimals to thousandths based on meanings of the digits in each place, using $>,=$, and $<$ <br> symbols to record the results of comparisons. |
| 5.NBT.4 | Use place value understanding to round decimals to any place. |
| 5.NBT.7 | Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and <br> strategies based on place value, properties of operations, and/or the relationship between addition and <br> subtraction; relate the strategy to a written method and explain the reasoning used. |

Mathematical Practices

K-12.MP. 1
Make sense of problems and persevere in solving them.

| K-12.MP3 | Construct viable arguments and critique the reasoning of others. |
| :---: | :---: |
| K-12.MP. 4 | Model with mathematics. |
| K-12.MP. 6 | Attend to precision. |
| K-12.MP. 8 | Look for and express regularity in repeated reasoning. |
| Interdisciplinary Connections |  |
| ELA |  |
| Math journal, math vocabulary discussions, reading topic-related books, providing explanations |  |
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| SL.1.3. | Ask and answer questions about what a speaker says in order to gather additional information or clarify something that is not understood. |
| SL.1.6. | Produce complete sentences when appropriate to task and situation. |
| Integration of Technology |  |
| Use of SmartBoard, playing online games |  |
| 8.1.2.A. 4 | Demonstrate developmentally appropriate navigation skills in virtual environments (i.e. games, museums). |
| Career Readiness, Life Literacies and Key Skills |  |
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| 9.2.5.CAP. 2 | Identify how you might like to earn an income. |
| 9.2.5.CAP. 3 | Identify qualifications needed to pursue traditional and non-traditional careers and occupations. |
| 9.2.5.CAP. 4 | Explain the reasons why some jobs and careers require specific training, skills, and certification (e.g., life guards, child care, medicine, education) and examples of these requirements. |


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| 9.4.5.TL. 1 | Compare the common uses of at least two different digital tools and identify the advantages and disadvantages of using each. |  |
| Instructional Focus |  |  |
| Enduring Understandings: |  | Essential Questions: |
| Decimals are another way of writing fractions or mixed numbers. <br> Thousandths can be represented with three decimal places or as fractions. <br> Decimals can be multiplied and divided in the same way as whole numbers. |  | How are fractions and decimals related? <br> How is multiplying and dividing different when working with decimals compared to when working with whole numbers? |
| Evidence of Learning (Assessments) |  |  |
| Math in Focus Assessment Guide Chapter 4: Decimals <br> Math in Focus Assessment Guide Chapter 5: Four Operations of Decimals Math in Focus Cumulative Review 2 (Chapters 4 and 5) <br> Benchmark Assessments |  |  |
| Objectives (SLO) |  |  |
| Students will <br> - Tho <br> - Equiv <br> - Est <br> - Div | now: | Students will be able to: <br> - Read and write thousandths in decimal and fraction forms. <br> - Represent and interpret thousandths in models or in place-value charts. <br> - Write a fraction with denominator 1,000 as a decimal. <br> - Compare and order decimals to 3 decimal places. <br> - Round decimals to the nearest hundredth. <br> - Rewrite decimals as fractions and mixed numbers in simplest form. |



Special Education - Reteach/Extra practice workbook pages, anchor charts, scaffolded explanations of topics, manipulatives, additional time for work, group work, visual aids, modeling, hands-on learning activities, small group work for more individualized attention
*These are only suggested ideas to modify instruction, modifications and accommodations should be tailored to each student's IEP and needs. Also, see textbook for Differentiated Instruction ideas in each chapter.

504 - Reteach/Extra practice pages, anchor charts, scaffolded explanations of topics, manipulatives, extra time for work, group work, visual aids, modeling, hands-on learning activities, small group work for more individualized attention

MLL - Select activities which reinforce chapter vocabulary and connections among these words such as:
A Word Wall which includes terms, definitions, and examples
Drawings and numbers to show examples of terms
Gifted and Talented - Enrichment workbook, Put on Your Thinking Cap pages and resources, higher-level questions, challenge packets, KenKen and other puzzles, leading group work

## Career Readiness, Life Literacies, and Key Skills NJSLS

Please select all standards that apply to this unit of study:
Act as a responsible and contributing community members and employee
Attend to financial well-being
Consider the environmental, social and economic impacts of decisions
Demonstrate creativity and innovation
Utilize critical thinking to make sense of problems and persevere in solving them
Model integrity, ethical leadership and effective management
Plan education and career paths aligned to personal goals
Use technology to enhance productivity increase collaboration and communicate effectively
Work productively in teams while using cultural/global competence
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| Unit 4 |
| :--- | :--- |
| $\quad$ Measurement \& Data |
| $\quad$ Summary and Rationale | | In this unit, students are introduced to three-dimensional solid shapes such as prisms, pyramids, cylinders, |
| :--- |
| spheres, and cones, and learn to recognize and identify the difference between these solid figures. Students |
| learn the fundamental concepts and vocabulary of solid shapes, such as vertex/vertices, edges, faces, and |
| bases. Models play an important role in the study of solids. Students see, touch, and manipulate models of |
| solids to consolidate their understanding. |
| Students build solids using unit cubes, draw cubes and rectangular prisms on dot paper, and find the volumes |
| of cubes, rectangular prisms, and liquids in rectangular containers. Students are expected to recognize area as |
| an attribute of two-dimensional shapes and volume as an attribute of three-dimensional shapes. |
| There are two different contexts to understand volume- the capacity of containers, and the amount of space |
| taken up by objects. Both of these contexts are explored in this unit. Volume is also measured using both |
| solid and liquid measures. |
| Students learn to make and interpret line plots to organize and represent data. |


| 5.MD.3a | A cube with side length 1 unit, called a "unit cube," is said to have "one cubic unit" of volume, and can be used to measure volume. |
| :---: | :---: |
| 5.MD.3b | A solid figure which can be packed without gaps or overlaps using $n$ unit cubes is said to have a volume of $n$ cubic units. |
| 5.MD. 4 | Measure volumes by counting unit cubes, using cubic cm , cubic in, cubic ft , and improvised units. |
| 5.MD. 5 | Relate volume to the operations of multiplication and addition and solve real world and mathematical problems involving volume. |
| 5.MD.5a | Find the volume of a right rectangular prism with whole-number side lengths by packing it with unit cubes, and show that the volume is the same as would be found by multiplying the edge lengths, equivalently by multiplying the height by the area of the base. Represent threefold whole-number products as volumes, e.g., to represent the associative property of multiplication. |
| 5.MD.5b | Apply the formulas $V=l \times w \times h$ and $V=b \times h$ for rectangular prisms to find volumes of right rectangular prisms with whole-number edge lengths in the context of solving real world and mathematical problems. |
| 5.MD.5c | Recognize volume as additive. Find volumes of solid figures composed of two non-overlapping right rectangular prisms by adding the volumes of the non-overlapping parts, applying this technique to solve real world problems. |
| Mathematica | ractices |
| K-12.MP. 1 | Make sense of problems and persevere in solving them. |
| K-12.MP. 2 | Reason abstractly and quantitatively. |
| K-12.MP3 | Construct viable arguments and critique the reasoning of others. |
| K-12.MP. 4 | Model with mathematics. |
| K-12.MP. 5 | Use appropriate tools strategically. |
| K-12.MP. 6 | Attend to precision. |
| K-12.MP. 8 | Look for and express regularity in repeated reasoning. |
| Interdisciplinary Connections |  |
| ELA |  |
| Math journal, math vocabulary discussions, reading topic-related books, providing explanations |  |


| SL.1.1. | Participate in collaborative conversations with diverse partners about grade 1 topics and texts with peers and adults in small and larger groups. A. Follow agreed-upon norms for discussions (e.g., listening to others with care, speaking one at a time about the topics and texts under discussion). B. Build on others' talk in conversations by responding to the comments of others through multiple exchanges. C. Ask questions to clear up any confusion about the topics and texts under discussion. |
| :---: | :---: |
| SL.1.3. | Ask and answer questions about what a speaker says in order to gather additional information or clarify something that is not understood. |
| SL.1.6. | Produce complete sentences when appropriate to task and situation. |
| Integration of Technology |  |
| Use of SmartBoard, playing online games |  |
| 8.1.2.A. 4 | Demonstrate developmentally appropriate navigation skills in virtual environments (i.e. games, museums). |
| Career Readiness, Life Literacies and Key Skills |  |
| 9.1.5.CR. 1 | Compare various ways to give back and relate them to your strengths, interests, and other personal factors. |
| 9.2.5.CAP. 1 | Evaluate personal likes and dislikes and identify careers that might be suited to personal likes. |
| 9.2.5.CAP. 2 | Identify how you might like to earn an income. |
| 9.2.5.CAP. 3 | Identify qualifications needed to pursue traditional and non-traditional careers and occupations. |
| 9.2.5.CAP. 4 | Explain the reasons why some jobs and careers require specific training, skills, and certification (e.g., life guards, child care, medicine, education) and examples of these requirements. |
| 9.2.5.CI. 3 | Participate in a brainstorming session with individuals with diverse perspectives to expand one's thinking about a topic of curiosity. |
| 9.2.5.CT. 1 | Identify and gather relevant data that will aid in the problem-solving process. |
| 9.2.5.CT. 2 | Identify a problem and list the types of individuals and resources (e.g., school, community agencies, governmental, online) that can aid in solving the problem. |
| 9.2.5.CT. 3 | Describe how digital tools and technology may be used to solve problems. |
| 9.2.5.CT. 4 | Apply critical thinking and problem-solving strategies to different types of problems such as personal, academic, community and global. |
| 9.4.5.IML. 2 | Create a visual representation to organize information about a problem or issue. |
| 9.4.5.IML. 3 | Represent the same data in multiple visual formats in order to tell a story about the data. |


| 9.4.5.TL. 1 Compare the common uses of at least t <br> disadvantages of using each | wo different digital tools and identify the advantages and |
| :---: | :---: |
| Instructional Focus |  |
| Enduring Understandings: | Essential Questions: |
| Solid figures can be identified and classified by the number of faces, edges, and vertices. <br> The volume of cubes and rectangular prisms can be expressed and the number of cubic units they contain. <br> Area is as an attribute of two-dimensional shapes and volume is as an attribute of three-dimensional shapes. <br> Volume is the capacity of containers, and is also the amount of space taken up by objects. <br> Volume is also measured using both solid and liquid measures. <br> Displaying data in a graph or line plot highlights some features of the data. <br> The horizontal axis of a line plot can contain fractional intervals. | How is the volume of any prism calculated? <br> How is volume different from surface area? <br> When is volume calculated in daily life? <br> How can we represent data in line plots? |
| Evidence of Learning (Assessments) |  |
| Math in Focus Assessment Guide Chapter 6: Volume Math in Focus Assessment Guide Chapter 7: Line Plots Math in Focus Cumulative Review 3 (Chapters 6 throu Benchmark Assessments |  |
| Objectives (SLO) |  |

Students will know:

- Face, base, edge, vertex
- Rectangular Prism
- Triangular prism
- Pyramid
- Square pyramid, triangular pyramid
- Net
- Cylinder
- Sphere
- Cone
- Right triangle
- Cube
- Unit cube
- Volume
- Capacity
- Volume formula
- Key
- Line plot

Students will be able to:

- Identify and classify prisms and pyramids.
- Identify the solid figure that can be formed from a net.
- Identify and classify cylinders, spheres, and cones.
- Identify rectangular prisms.
- Build solids using unit cubes.
- Determine the number of unit cubes in an irregular solid.
- Draw a cube and a rectangular prism on dot paper.
- Complete a partially drawn cube and rectangular prism on dot paper.
- Find the volumes of cubes and rectangular prisms.
- Find the volume of a solid constructed by unit cubes.
- Compare volumes of cubes, rectangular prisms, and other objects.
- Use a formula to find the volume of a rectangular prism.
- Find the capacity of a rectangular container.
- Find the volume of a figure composed of two rectangular prisms.
- Solve word problems involving volumes of rectangular prisms, liquids, and of figures composed of two rectangular prisms.
- Make a line plot to represent data given in fractions of a unit.
- Use operations on fractions to solve problems on the information presented.


## Suggested Resources/Technology Tools

## Math in Focus Resources Chapter 6: Volume

Math in Focus Resources Chapter 7 Part 1: Line Plots

## Resources and Manipulatives

Solid shapes
Number cubes
Net of solid shapes
Connecting cubes
Dot paper
Containers

Online Resources
HMH Ed: Your Friend in Learning
www.mathsisfun.com/geometry/prisms.html (Volume of right prisms -Notes and practice)
www.mrnussbaum.com/coolgraphing.htm (Several graphs to practice organizing data)

Literacy Connections

## Tier 1 Modifications and Accommodations

Including special education students, Multilingual Language Learners (MLLs), students at risk of school failure, gifted and talented students, and students with 504 plans;

## General Modifications for students struggling to learn:

Small group instruction within the classroom
Differentiation through content, process, product, and environment
Individual feedback and praise towards what is done correctly based upon effort, attitude and strategy.
Help students manage individual stressors for the student and plan alternate pathways for completion of assignments
Special Education - Reteach/Extra practice workbook pages, anchor charts, scaffolded explanations of topics, manipulatives, additional time for work, group work, visual aids, modeling, hands-on learning activities, small group work for more individualized attention.
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Attend to financial well-being
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| Unit 5 |
| :--- | :--- |
| Geometry |
| Summary and Rationale | | In this unit, students learn how to plot and identify points on a coordinate plane. They learn to read and plot |
| :--- |
| points on a coordinate plane, and then look for patterns that may represent a relationship between two |
| number sets. |
| Students learn the properties of polygons, particularly triangles and quadrilaterals. They learn to identify |
| special triangles such as right, isosceles, and equilateral triangles, categorized by angle measures and/or side |
| lengths. Students also learn to classify polygons based on a hierarchy according to their attributes. |


|  | graph the ordered pairs on a coordinate plane. |
| :---: | :---: |
| Mathematical Practices |  |
| K-12.MP. 1 | Make sense of problems and persevere in solving them. |
| K-12.MP. 2 | Reason abstractly and quantitatively. |
| K-12.MP3 | Construct viable arguments and critique the reasoning of others. |
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| :---: | :---: | :---: |
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| 9.2.5.CAP. 3 | Identify qualifications needed to pursue traditional and non-traditional careers and occupations. |  |
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| 9.4.5.TL. 1 | Compare the common uses of at least two different digital tools and identify the advantages and disadvantages of using each. |  |
| Instructional Focus |  |  |
| Enduring U | erstandings: | Essential Questions: |
| A coordina number line the x -axis. $y$-axis. The origin. <br> Points on a an ordered pair gives while the $y$ of the point <br> Plotted poin relationship <br> Polygons properties | plane is the intersection of two The horizontal number line is called vertical number line is called the int where they intersect is called the ordinate plane are identified using r. The x-coordinate of the ordered horizontal location of the point ordinate gives the vertical location <br> on a coordinate plane often show a etween two sets of numbers. <br> be classified according to their mber of sides, angle types, etc.) | How can you describe a point on a coordinate plane? <br> How can you use the coordinate plane to show number patterns? <br> What properties can you use to identify a type of triangle? <br> In what ways can triangles be classified? <br> How can you classify polygons using a hierarchy? <br> In what ways can quadrilaterals be classified? <br> Why isn't a trapezoid classified as a parallelogram? |

Triangles and four-sided figures have their own special properties.

Triangles can be classified by their side lengths and by their angle measures and by their sides.

A scalene triangle is a triangle with no equal angles or sides.
An isosceles triangle is a triangle with two equal sides (legs) and two equal angles (base angles).
An equilateral triangle is a triangle with three equal sides and three equal angles.

A parallelogram is a four-sided figure (a quadrilateral) with two pairs of opposite sides that are parallel and equal. Opposite angles of a parallelogram are equal.
A rectangle is a parallelogram with four right angles.
A rhombus is a parallelogram with four equal sides.
A square is a parallelogram with four right angles and four equal sides.

A trapezoid is a four-sided figure (a quadrilateral) with one pair of opposite sides. (Therefore, a trapezoid is not a parallelogram.

The graph of an equation on a coordinate grid often represents a functional relationship between two quantities.

Evidence of Learning (Assessments)

Math in Focus Assessment Guide Chapter 7 Part 2: The Coordinate Plane
Math in Focus Assessment Guide Chapter 8: Polygons
Math in Focus Cumulative Review 3 (Chapters 6 through 8)
Benchmark Assessments
Objectives (SLO)

Students will know:

- Coordinate grid, coordinate plane
- X-axis, y-axis
- Ordered pair
- x-coordinate, y-coordinate
- Origin
- Equilateral triangle
- Isosceles triangle
- Scalene triangle
- Right triangle
- Acute triangle
- Obtuse triangle
- Polygon
- Regular polygon
- Kite
- Heptagon
- Octagon
- Nonagon
- Decagon
- Quadr
- Parallelogram
- Rhombus
- Trapezoid
- Rectangle
- Square

Students will be able to:

- Read and plot points on a coordinate plane.
- Use ordered pairs to draw line graphs.
- Look for and extend number patterns.
- Identify The relationship between two sets of numbers.
- Identify isosceles, equilateral, and scalene triangles
- Classify triangles by the lengths of their side lengths and angle measures.
- Understand and apply the properties of right, isosceles, and equilateral triangles
- Classify polygons using a hierarchy.
- Understand and apply the properties of parallelograms, rhombuses, and trapezoids.


## Suggested Resources/Technology Tools

Math in Focus Resources Chapter 7 Part 2: The Coordinate Plane
Math In Focus Resources Chapter 8: Polygons

Resources and Manipulatives

Graphs
Rulers
Coordinate grids
Grid paper
Protractors
Inch and centimeter rulers
Tracing paper
Drawing triangles
Shape cut-outs

Online Resources
HMH Ed: Your Friend in Learning
www.mathplayground.com/locate_aliens.html (Coordinates)

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